

- Definitions:

$$\left. \frac{df}{dx} \right|_a = \frac{df}{dx}(a) = f'(a) = \lim_{h \rightarrow 0} \frac{f(a+h) - f(a)}{h}$$

$$\frac{d}{dx} f(x) = f'(x) = \lim_{h \rightarrow 0} \frac{f(x+h) - f(x)}{h}$$

- General Rules:

$$\frac{d}{dx} [af(x) \pm bg(x)] = af'(x) \pm bg'(x) \quad a \text{ and } b \text{ fixed constants}$$

Product rule:

$$\frac{d}{dx} [f(x)g(x)] = f'(x)g(x) + f(x)g'(x) \quad (fg)' = f'g + fg'$$

Quotient rule:

$$\frac{d}{dx} \left[\frac{f(x)}{g(x)} \right] = \frac{f'(x)g(x) - f(x)g'(x)}{g^2(x)} \quad \left(\frac{f}{g} \right)' = \frac{f'g - fg'}{g^2}$$

Chain rule:

$$\frac{d}{dx} [f(g(x))] = f'(g(x))g'(x) \quad \frac{d}{dx} f(u) = f'(u)u'$$

$$\frac{d}{dx} f(u) = \left. \frac{df}{du} \right|_{u(x)} \frac{du}{dx} \quad \frac{d}{dx} f(u) = \frac{df}{du} \frac{du}{dx}$$

- Specific functions:

$$\frac{d}{dx} x^p = px^{p-1} \quad \frac{d}{dx} x = 1 \quad \frac{d}{dx} c = 0$$

$$\frac{d}{dx} \sin(x) = \cos(x) \quad \frac{d}{dx} \cos(x) = -\sin(x)$$

$$\frac{d}{dx} \tan(x) = \sec^2(x) \quad \frac{d}{dx} \cot(x) = -\csc^2(x)$$

$$\frac{d}{dx} \sec(x) = \sec(x) \tan(x) \quad \frac{d}{dx} \csc(x) = -\csc(x) \cot(x)$$

$$\frac{d}{dx} e^x = e^x \quad \frac{d}{dx} a^x = a^x \ln(a)$$

$$\frac{d}{dx} \ln(x) = \frac{1}{x} \quad \frac{d}{dx} \log_b(x) = \frac{1}{x \ln(b)}$$

$$\frac{d}{dx} \sin^{-1}(x) = \frac{1}{\sqrt{1-x^2}} \quad \frac{d}{dx} \cos^{-1}(x) = \frac{-1}{\sqrt{1-x^2}}$$

$$\frac{d}{dx} \tan^{-1}(x) = \frac{1}{1+x^2} \quad \frac{d}{dx} \cot^{-1}(x) = \frac{-1}{1+x^2}$$

$$\frac{d}{dx} \sec^{-1}(x) = \frac{1}{x\sqrt{x^2-1}} \quad \frac{d}{dx} \csc^{-1}(x) = \frac{-1}{x\sqrt{x^2-1}}$$

- Generalizations (assume $u = u(x)$):

$$\frac{d}{dx}u^p = pu^{p-1}\frac{du}{dx}$$

$$\frac{d}{dx}\sqrt{u} = \frac{1}{2\sqrt{u}}\frac{du}{dx} = \frac{u'}{2\sqrt{u}}$$

$$\frac{d}{dx}\sin(u) = \cos(u)\frac{du}{dx}$$

$$\frac{d}{dx}\cos(u) = -\sin(u)\frac{du}{dx}$$

$$\frac{d}{dx}\tan(u) = \sec^2(u)\frac{du}{dx}$$

$$\frac{d}{dx}\cot(u) = -\csc^2(u)\frac{du}{dx}$$

$$\frac{d}{dx}\sec(u) = \sec(u)\tan(u)\frac{du}{dx}$$

$$\frac{d}{dx}\csc(u) = -\csc(u)\cot(u)\frac{du}{dx}$$

$$\frac{d}{dx}e^u = e^u\frac{du}{dx} = u'e^u$$

$$\frac{d}{dx}e^{cx} = ce^{cx}$$

$$\frac{d}{dx}\ln(u) = \frac{1}{u}\frac{du}{dx} = \frac{u'}{u}$$

$$\frac{d}{dx}\ln(cx) = \frac{1}{x}$$

$$\frac{d}{dx}a^u = a^u \ln(a)\frac{du}{dx}$$

$$\frac{d}{dx}\log_b(u) = \frac{1}{u \ln(b)}\frac{du}{dx}$$

$$\frac{d}{dx}\sin^{-1}(u) = \frac{1}{\sqrt{1-u^2}}\frac{du}{dx}$$

$$\frac{d}{dx}\cos^{-1}(u) = \frac{-1}{\sqrt{1-u^2}}\frac{du}{dx}$$

$$\frac{d}{dx}\tan^{-1}(u) = \frac{1}{1+u^2}\frac{du}{dx}$$

$$\frac{d}{dx}\cot^{-1}(u) = \frac{-1}{1+u^2}\frac{du}{dx}$$

$$\frac{d}{dx}\sec^{-1}(u) = \frac{1}{u\sqrt{u^2-1}}\frac{du}{dx}$$

$$\frac{d}{dx}\csc^{-1}(u) = \frac{-1}{u\sqrt{u^2-1}}\frac{du}{dx}$$

It's implied that we are working within the domain of the original function. For example, $u > 0$ for $\ln(u)$, $|u| \leq 1$ for $\sin^{-1}(u)$, $|u| \geq 1$ for $\sec^{-1}(u)$, etc.